

CH.6 WS #3 Calculus BC

Name _____ Per. _____

1) Given $\frac{dy}{dx} = 3(8 - y)$ with initial condition $(0, 6)$.

a) Find the particular solution of the differential equation.

b) Use Euler's method with step size $h = 0.5$ to approximate $y(1)$.

c) Use tangent line at $(0, 6)$ to approximate $f(1)$.

d) Find $y(1)$.

2) A population of elk is represented by the logistic differential equation $\frac{dP}{dt} = \frac{P}{20} - \frac{P^2}{10000}$

a) Find the value of k and the carrying capacity.

$$k = \underline{\hspace{2cm}} \quad L = \underline{\hspace{2cm}}$$

b) The initial population is $P(0) = 100$ elk.

$$P(t) =$$

Find a formula for the population in terms of t .

$$\underline{\hspace{4cm}}$$

c) What is the elk population when the growth rate is at its maximum?

$$P = \underline{\hspace{2cm}}$$

d) How long will it take for the elk population to reach the amount in part c?

$$t = \underline{\hspace{2cm}}$$

e) How long will it take for the elk population to reach 700?

$$t = \underline{\hspace{2cm}}$$

f) What is the elk population after 75 years?

$$P = \underline{\hspace{2cm}}$$

3) A sadistic organization releases 300 foxes into a preserve. After 3 years, there are 250 foxes in the preserve. The preserve has a carrying capacity of 200.

a) Write a logistic equation that models the population.

b) What is $\lim_{t \rightarrow \infty} P(t)$?

c) What is the population after 10 years?

d) What is the population after 25 years?