Formula for Arclength
(Function notation)

$$
y=f(x)
$$

Formula for Arclength or Distance travelled (Parametric)

Formula for Speed (Parametric)

Formula for Slope (Parametric)

## Integration by Parts

What is the name of the shortcut that we use in place of Integration by Parts?

What is my first step in this problem?

$$
\int \frac{4 x^{2}+2}{x^{2}-7} d x
$$

| $L=\int_{a}^{b} \sqrt{\left(\frac{d x}{d t}\right)^{2}+\left(\frac{d y}{d t}\right)^{2}} d t$ | $L=\int_{a}^{b} \sqrt{1+\left(f^{\prime}(x)\right)^{2}} d x$ |
| :---: | :---: |
| $\frac{d y / d t}{d x / d t} \frac{d y}{d x}=s l o p e$ |  |
|  |  |
| $A=\frac{1}{2} \cdot \int_{a}^{b} r^{2} d \theta$ | Speed $=\sqrt{\left(\frac{d x}{d t}\right)^{2}+\left(\frac{d y}{d t}\right)^{2}}$ |
|  |  |
|  |  |
|  |  |

Which technique is used to solve this problem?

$$
\int \frac{8}{(x-4)(x+3)} d x
$$

Which technique is used to solve this problem?

$$
\int \ln x d x
$$

Which technique is used to solve this problem?

$$
\int x \sqrt{x^{2}+3} d x
$$

What is my first step in this problem

$$
\frac{d y}{d x}=4 x y
$$

if looking for original equation?

When does
L'Hopital's Rule apply?

What is L'Hopital's Rule?

What is Taylor's theorem for approximating $f(x)$ to the nth term?

## Integration by Parts

## Partial Fractions

New $y=$ Old $y+d x \cdot \frac{d y}{d x}$
$d x$ : change in $x$
$\frac{d y}{d x}=$ Derivative (slope) at the point.

## Substitution

$$
\lim _{x \rightarrow a} \frac{f(x)}{g(x)}=\lim _{x \rightarrow a} \frac{f^{\prime}(x)}{g^{\prime}(x)}
$$

## Separate the variables

$$
\begin{aligned}
f(x)= & f(c)+\frac{f^{\prime}(c)}{1!}(x-c)+\frac{f^{\prime \prime}(c)}{2!}(x-c)^{2}+ \\
& \ldots \ldots+\frac{f^{n}(c)}{n!}(x-c)^{n}
\end{aligned}
$$

If the limit is of the form $\frac{0}{0}$ or $\frac{\infty}{\infty}$.

## MacLaurin Series are centered at ...

The MacLaurin Series for $\boldsymbol{e}^{x}$ is....

The MacLaurin Series for $\sin x$ is....

The MacLaurin Series for $\cos x$ is....

Formulas for Hooke's Law

Area as a limit

Formulas for Logistical Growth

Series for $e^{x}: \quad=1+x+\frac{x^{2}}{2!}+\frac{x^{3}}{3!}+$

$$
c=0
$$

Series for $\cos x:=1-\frac{x^{2}}{2!}+\frac{x^{4}}{4!}-\ldots$
Series for $\sin x:=x-\frac{x^{3}}{3!}+\frac{x^{5}}{5!}-\ldots$

The force $F$ required to compress a spring

$$
\frac{d y}{d t}=k y\left(1-\frac{y}{L}\right) ; y=\frac{L}{1+b e^{-k t}} \quad ; \quad b=\frac{L-Y_{0}}{Y_{0}}
$$

where $L$ is the carrying capacity and $k$ is the constant of proportionality is proportional to the distance $d$ the spring is compressed or stretched from its' original length.

$$
\begin{gathered}
F=k d \\
W=\int_{a}^{b} k x d x \\
k=\text { constant of proportionality }
\end{gathered}
$$

## Improper Integral

Area $=\lim _{n \rightarrow \infty} \sum_{i=1}^{n} f\left(a+\frac{b-a}{n} i\right)\left(\frac{b-a}{n}\right)$
height width $i=$ interval

Tell whether this series is convergent or divergent and

$$
\begin{gathered}
\text { why? } \\
\sum_{n=1}^{\infty} \frac{1}{n}-\frac{1}{n+1}
\end{gathered}
$$

Tell whether this series is convergent or divergent and why?

$$
\sum_{n=1}^{\infty} \frac{(-1)^{n} 7^{n}}{5^{n}}
$$

Tell whether this series is convergent or divergent and why?

$$
\sum_{n=1}^{\infty} \frac{(-1)^{n} n!}{e^{n}}
$$

Tell whether this series is convergent or divergent and why?

$$
\sum_{n=1}^{\infty} \frac{(-1)^{n}}{n+1}
$$

Tell whether this series is convergent or divergent and

$$
\begin{gathered}
\text { why? } \\
\sum_{n=2}^{\infty} \frac{n^{3}+2}{n^{3}-5}
\end{gathered}
$$

Tell whether this series is convergent or divergent and why?

$$
\sum_{n=1}^{\infty} 5\left(\frac{2}{3}\right)^{n}
$$

Tell whether this series is convergent or divergent and

$$
\begin{aligned}
& \text { why? } \\
& \sum_{n=1}^{\infty} \frac{1}{n^{1.4}}
\end{aligned}
$$

1
$\overline{1-x}$ is

| Diverges by Root Test | Converges by Telescoping Series |
| :---: | :---: |
| Converges by Alternating Series | Diverges by Ratio Test |
| Converges by p-series | Diverges by nth-term Test |
| Series for $\frac{1}{1-x}:=1+x+x^{2}+x^{3} \ldots$ | Converges by Geometric series |


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